

## Assignment 7: The Adventures of Links

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*"Splicing and Dicing" assignment inspired by an assignment by Owen Astrachan entitled "DNA Splicing."  
Thanks to Julie Zelenski, Katherine Erdman, Max Darling, Maya Ziv, Richard Lin, and Trip Master for their input on this assignment!*

Linked structures are a fundamentally different way of encoding sequences than the array-based approaches you worked with on Assignment 5 and Assignment 6. This assignment is all about manipulating, traversing, and exploring linked structures. It's a two-parter. The first part is a hybrid coding/debugging exercise where you'll work the debugger to escape from a maze. The second part is a coding exercise in which you'll use linked lists to manipulate DNA sequences.

***Due Friday, March 6<sup>th</sup> at 11:30AM.***

***You are welcome to work in pairs on this assignment.***

You know the drill – make consistent, slow, steady progress on this assignment rather than doing everything at the last minute. Here's our recommended timeline:

- Aim to complete The Labyrinth! within two days of this assignment going out.
- Aim to complete Splicing and Dicing within seven days of this assignment going out.

A reminder: you cannot use late days on the assignment that goes out after this one, so if you do end up using late days here, you will cut into the time you would otherwise have to work on the final assignment. Use late days if you need to, but be careful not to fall too far behind.

## Problem One: The Labyrinth!

You have been trapped in a labyrinth, and your only hope to escape is to cast the magic spell that will free you from its walls. To do so, you will need to explore the labyrinth to find three magical items:

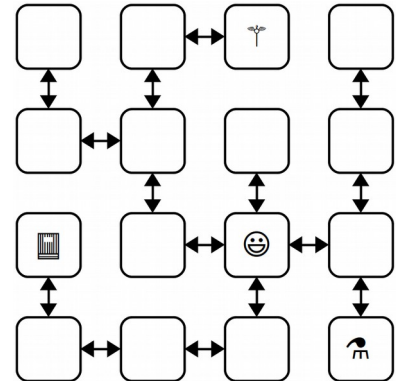
- The *Spellbook* (📖), which contains the spell you need to cast to escape.
- The *Potion* (🧪), containing the arcane compounds that power the spell.
- The *Wand* (🪄), which concentrates your focus to make the spell work.

Once you have all three items, you can cast the spell to escape to safety.

This is, of course, no ordinary maze. It's a *pointer maze*. The maze consists of a collection of objects of type `MazeCell`, where `MazeCell` is defined here:

```
struct MazeCell {
    string whatsHere; // One of "", "Spellbook", "Potion", or "Wand"
    MazeCell* north; // The cell north of us, or nullptr if we can't go north.
    MazeCell* south;
    MazeCell* east;
    MazeCell* west;
};
```

For example, to the right is a  $4 \times 4$  labyrinth. We've marked your starting position with a smiley face and the positions of the three items with similarly cute emojis. The `MazeCell` you begin at would have its north, south, east, and west pointers pointing at the `MazeCell` objects located one step in each of those directions from you. On the other hand, the `MazeCell` containing the book would have its north, east, and west pointers set to `nullptr`, and only its south pointer would point somewhere (specifically, to the cell in the bottom-left corner).



Each `MazeCell` has a variable named `whatsHere` that indicates what item, if any, is at that position. Empty cells will have `whatsHere` set to the empty string. The cells containing the Spellbook, Potion, or Wand will have those fields set to "Spellbook", "Potion", and "Wand", respectively, with that exact capitalization.

If you were to find yourself in this labyrinth, you could walk around a bit to find the items you need to cast the escape spell. There are many paths you can take; here's three of them:

ESNWWNNEWSSESWWN    SWWNSEENWNNEWSSEES    WNNEWSSESWWNSEENES

Each path is represented as a sequence of letters (N for north, W for west, etc.) that, when followed from left to right, trace out the directions you'd follow. For example, the first sequence represents going east, then south (getting the Potion), then north, then west, etc. Trace though those paths and make sure you see how they pick up all three items.

There are three milestones to this problem. The first one is a coding problem, and the second two are debugger exercises. We strongly recommend completing them in the order in which they appear, as they build on top of one another.

## Milestone 1: Check Paths to Freedom

Your first task is to write a function that, given a cell in a maze and a path, checks whether that path is legal and picks up all three items. Specifically, in the file `Labyrinth.cpp`, implement the function

```
bool isPathToFreedom(MazeCell* startLocation, const string& path);
```

This function takes as input your starting location in the maze and a string made purely from the characters 'N', 'S', 'E', and 'W', then returns whether that path lets you escape from the maze.

A path lets you escape the maze if (1) the path is legal, in the sense that it never takes a step that isn't permitted in the current `MazeCell`, and (2) the path picks up the Spellbook, Wand, and Potion. The order in which those items are picked up is irrelevant, and it's okay if the path continues onward after picking all the items up.

You can assume that `startLocation` is not a null pointer (you do indeed begin somewhere). However, if the input string contains any invalid characters (that is, characters other than 'N', 'S', 'E', or 'W'), you should use the `error()` function to report an error.

To summarize:

1. Implement the `isPathToFreedom` function in `Labyrinth.cpp`.
2. Test your code thoroughly using our provided tests. (If you'd like to write tests of your own, you're welcome to do so, though it's not required here.)

Some notes on this problem:

- Every maze cell's `what'sHere` field will contain exactly one of the four options indicated earlier ("", "Spellbook", "Wand", and "Potion"). You don't need to worry about the case where the maze contains items other than these. We could have conceivably used an enumerated type to represent this (see Chapter 1.6 of the textbook for more on enumerated types), but figured it would be easier to just use strings here.
- Your code should work for a `MazeCell` from any possible maze, not just the one shown on the previous page.
- Although in the previous picture the maze was structured so that if there was a link from one cell to another going north there would always be a link from the second cell back to the first going south (and the same for east/west links), you should *not* assume this is the case in this function. Then again, chances are you wouldn't need to assume this.
- You shouldn't need to allocate any new `MazeCell` objects in the course of solving this problem. Feel free to declare variables of type `MazeCell*`, but don't use the `new` keyword. After all, your job is to check a path in an existing maze, not to make a new maze.

## ***Milestone 2: Escape from Your Personal Labyrinth***

Your next task is to escape from a labyrinth that's specifically constructed for you (and your partner, if you're working in a pair). The starter code we've provided will use your name(s) to build you a personalized labyrinth. By "personalized," we mean "no one else in the course is going to have the exact same labyrinth as you." Your job is to figure out a path through that labyrinth that picks up all the three items, allowing you to escape.

Open the file `LabyrinthEscape.cpp` and you'll see three constants. The first one, `kYourName`, is a spot for your name (or your name and your partner's name, if you're working in a pair). Right now, it's marked with a `TODO` message. Edit this constant so that it contains your name(s).

Scroll down to the *first* test case in `LabyrinthEscape.cpp`. This test case generates a personalized labyrinth based on the `kYourName` constant and returns a pointer to one of the cells in that maze. It then checks whether the constant `kPathOutOfNormalMaze` is a sequence that will let you escape from the maze. Right now, `kPathOutOfNormalMaze` is a `TODO` message, so it's not going to let you escape from the labyrinth. You'll need to edit this string with the escape sequence once you find it.

To come up with a path out of the labyrinth, use the debugger! Set a breakpoint at the indicated line in the *first* test case. Launch the demo app with the debugger enabled and hit "Run Tests." When you do, you should see the local variables window pop up, along with the contents of `startLocation`, which is the `MazeCell` where we've dropped you into the labyrinth. Clicking the dropdown triangle in the debugger window will let you read the contents of the `whatsHere` field of `startLocation` (it'll be empty), as well as the four pointers leading out of the cell.

Depending on your maze, you may find yourself in a position where you can move in all four cardinal directions, or you may find that you can only move in some of them. The pointers in directions you can't go are all equal to `nullptr`, which will show up as `0x0` in the debugger window. The pointers that indicate directions you can go will all have dropdown arrows near them. Clicking one of these arrows will show you the `MazeCells` reachable by moving in the indicated directions. You can navigate the maze further by choosing one of those dropdown arrows, or you could back up to the starting maze cell and explore in other directions. It's really up to you!

***Draw a lot of pictures.*** Grab a sheet of paper and map out the maze you're in. There's no guarantee where you begin in the maze – you could be in the upper-left corner, dead center, etc. The items are scattered randomly, and you'll need to seek them out. Once you've mapped out the maze, construct an escape sequence and stash it in the constant `kPathOutOfNormalMaze`, then see if you pass the first test. If so, fantastic! You've escaped! If not, you have lots of options. You could step through your `isPathToFreedom` function to see if one of the letters you entered isn't what you intended and accidentally tries to move in an illegal direction. Or perhaps the issue is that you misdrew your map and you've ended up somewhere without all the items. You could alternatively set the breakpoint at the test case again and walk through things a second time, seeing whether the picture of the maze you drew was incorrect.

To summarize, here's what you need to do:

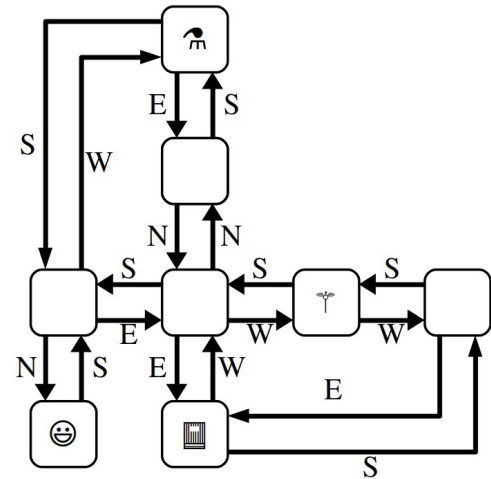
1. Edit the constant `kYourName` at the top of `LabyrinthEscape.cpp` with a string containing your name and your partner's name if you're working in a group. ***Don't skip this step!*** If you forget to do this, you'll be solving the wrong maze!
2. Set a breakpoint at the indicated line in the *first* test case in `LabyrinthEscape.cpp`, run the program in debug mode, and choose "Run Tests" to activate the breakpoint.
3. Map out the maze on a sheet of paper and find where all the items are. Once you're done, stop the running program.
4. Find a path that picks up all three items and edit the constant `kPathOutOfNormalMaze` at the top of `LabyrinthEscape.cpp` with that path. Run the test a second time with the debugger turned off to confirm you've escaped.

### Milestone 3: Escape from Your Personal Twisty Labyrinth

Now, let's make things a bit more interesting. In the previous section, you escaped from a labyrinth that nicely obeyed the laws of geometry. The locations you visited formed a nice grid, any time you went north you could then go back south, etc.

In this section, we're going to relax these constraints, and you'll need to find your way out of trickier mazes that look like the one shown to the right.

This maze is stranger than the previous one you explored. For example, you'll notice that these `MazeCell`s are no longer in a nice rectangular grid where directions of motion correspond to the natural cardinal directions. There's a `MazeCell` here where moving north and then north again will take you back where you started. In one spot, if you move west, you have to move *south* to return to where you used to be. In that sense, the names "north," "south," "east," and "west" here no longer have any nice geometric meaning; they're just the names of four possible exits from one `MazeCell` into another.



The one guarantee you do have is that if you move from one `MazeCell` to a second, there will always be a direct link from the second cell back to the first. It just might be along a direction of travel that has no relation to any of the directions you've taken so far.

The *second* test case in `LabyrinthEscape.cpp` contains code that generates a twisty labyrinth personalized with the `kYourName` constant. As before, you'll need to find a sequence of steps that will let you collect the three items you need to escape.

In many regards, the way to complete this section is similar to the way to complete the previous one. Set a breakpoint in the indicated spot in the second test case and use the debugger to explore the maze. Unlike the previous section, though, in this case you can't rely on your intuition for what the geometry of the maze will look like. For example, suppose your starting location allows you to go north. You might find yourself in a cell where you can then move either east or west. One of those directions will take you back where you started, but how would you know which one?

This is where memory addresses come in. Internally, each object in C++ has a *memory address* associated with it. Memory addresses typically are written out in the form `@0xsomething`, where *something* is the address of the object. You can think of memory addresses as sort of being like an "ID number" for an object – each object has a unique address, with no two objects having the same address. When you pull up the debugger view of a maze cell, you should see the `MazeCell` memory address under the Value column.

For example, suppose that you're in a maze and your starting location has address `0x7fffc8003740` (the actual number you see will vary based on your OS), and you can move to the south (which ways you can go are personalized to you based on your name, so you may have some other direction to move). If you expand out the dropdown for the south pointer, you'll find yourself at some other `MazeCell`. One of the links out of that cell takes you back where you've started, and it'll be labeled `0x7fffc8003740`. Moving in that direction might not be productive – it just takes you back where you came from – so you'd probably want to explore other directions to search the maze.

It's going to be hard to escape from your maze unless you *draw lots of pictures* to map out your surroundings. To trace out the maze that you'll be exploring, we recommend diagramming it on a sheet of paper as follows. For each `MazeCell`, draw a circle labeled with the memory address, or, at least the last five characters of that memory address. (Usually, that's sufficient to identify which object you're looking at). As you explore, add arrows between those circles labeled with which direction those arrows correspond to. What you have should look like the picture above, except that each circle will be annotated with a memory address. It'll take some time and patience, but with not too much effort you should be able to scout out the full maze. Then, as before, find an escape sequence from the maze!

To recap, here's what you need to do:

1. Set a breakpoint at the indicated line in the *second* test case in `LabyrinthEscape.cpp`, run the demo app in debug mode and choose "Run Tests" to activate the breakpoint.
2. Map out the twisty maze on a sheet of paper and find where all the items are and how the cells link to each other. Once you're done, stop the running program.
3. Find an escape sequence, and edit the constant `kPathOutOfTwistyMaze` at the top of `LabyrinthEscape.cpp` with that constant. Run the tests again – this time without the breakpoint – and see if you've managed to escape!

Some notes on this problem:

- ***The memory addresses of objects are not guaranteed to be consistent across runs of the program.*** This means that if you map out your maze, stop the running program, and then start the program back up again, you are *not* guaranteed that the addresses of the `MazeCells` in the maze will be the same. The *shape* of the maze is guaranteed to be the same, though. If you do close your program and then need to explore the maze again, you may need to relabel your circles as you go, but you won't be drawing a different set of circles or changing where the arrows link.
- You are guaranteed that if you follow a link from one `MazeCell` to another, there will always be a link from that second `MazeCell` back to the first, though the particular directions of those links might be completely arbitrary. That is, you'll never get "trapped" somewhere where you can move one direction but not back where you started.
- Attention to detail is key here – different `MazeCell` objects will always have different addresses, but those addresses might be really similar to one another. Make sure that as you're drawing out your diagram of the maze, you don't include duplicate copies of the same `MazeCell`.
- The maze you're exploring might contain loops or cases where there are multiple distinct paths between different locations. Keep this in mind as you're exploring or you might find yourself going in circles!
- Remember that you don't necessarily need to map out the whole maze. You only need to explore enough of it to find the three items and form a path that picks all of them up.

At this point, you have a solid command of how to use the debugger to analyze linked structures. You know how to recognize a null pointer, how to manually follow links between objects, and how to reconstruct the full shape of the linked structure even when there's bizarre and unpredictable cross-links between them. We hope you find these skills useful as you continue to write code that works on linked lists and other linked structures!

## Problem Two: Splicing and Dicing

DNA strands are made up of smaller units called *nucleotides*. There are four different nucleotides present in DNA, which are represented by the letters A, C, G, and T. Any DNA strand, therefore, can be thought of as linked structure consisting of the nucleotides that make up that strand, in order. In software, we might represent a nucleotide as a doubly-linked list made of individual units that look like this:

```
struct Nucleotide {  
    char value; // 'A', 'C', 'G', or 'T'  
    Nucleotide* next;  
    Nucleotide* prev;  
};
```

For example, the DNA sequence TAGCAT would be represented as follows:



Although they aren't pictured here, the `prev` pointer of the first T and the `next` pointer of the last T would each be set to `nullptr`. For visual simplicity, we're going to leave those pointers out of future pictures as well, but it doesn't hurt to draw them in!

There are four milestones in this part of the assignment, and they're spelled out over the next pages.

### ***Milestone One: Implement Core Functions***

Your first task is to write functions for manipulating existing DNA sequences. First, write a function

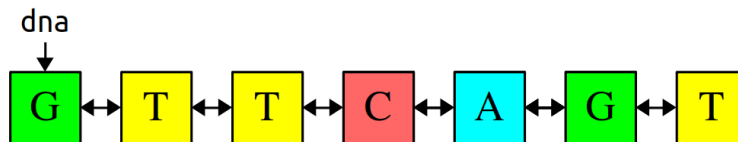
```
void deleteNucleotides(Nucleotide* dna);
```

that takes as input a pointer to a DNA strand, then deletes all the memory used by the nucleotides in that strand. It's possible that the input pointer is `nullptr` if the DNA strand is empty, in which case this function should do nothing.

Next, write this function:

```
string fromDNA(Nucleotide* dna);
```

This function takes as input a sequence of nucleotides, then returns a string representation of the DNA strand. For example, calling `fromDNA` on the `dna` pointer shown below would return "GTTTCAGT":



With that in mind, here's your first milestone:

#### ***Milestone 1: Implement Core Functions***

1. Add at two custom test cases to `SplicingAndDicing.cpp`, one for each of the functions mentioned above.
2. Implement the `deleteNucleotides` function and test it thoroughly.
3. Implement the `fromDNA` function and test it thoroughly.

Some notes on this problem:

- **Draw pictures!** Get out a pencil and paper and trace out what operations you want to perform on your linked lists before you write any code. Then, as you're writing up the code, refer back to your pictures to make sure each line of code does what you want it to do.
- If you leave a pointer uninitialized in C++, it does *not* default to `nullptr` and instead points somewhere random. Using a pointer like this will almost certainly crash your program immediately. It's a good idea to explicitly set pointers you don't want pointing at anything to `nullptr`.
- Your implementations of these functions should run in time  $O(n)$ . If you're able to pass the provided stress tests, with each one taking at most a few seconds, you should be in good shape.
- These functions must work correctly on large inputs. This likely means that you won't be able to implement them recursively, since doing so would lead to stack overflows on long strands.
- You can assume these functions always take in a pointer to the first nucleotide in the strand (or `nullptr` if the strand is empty). You don't need to handle pointers into the middle of lists.
- You should not allocate any memory with `new` in the course of implementing these functions, since you're not actually creating any new nucleotides. Feel free to declare variables of type `Nucleotide*` (remember that creating a pointer is separate from requesting space using the `new` operator), but don't use the `new` operator.
- You **must not** use any of the container types (e.g. `Vector`, `HashSet`, etc.) in the your solutions. See if you can do this purely using linked lists.



## Milestone Two: Construct New Sequences

Your next task is to write a function

```
Nucleotide* toStrand(const string& dna);
```

This function takes in a string representing a DNA strand and returns a chain of `Nucleotides` encoding that DNA strand. You can think of it as the inverse of the `fromDNA` function: `fromDNA` takes in a `Nucleotide*` and returns a `string`, while `toStrand` takes in a `string` and returns a `Nucleotide*`.

For example, calling `toStrand("TAGCAT")` should return the a pointer to the first nucleotide in the DNA strand shown below:



Here's what you need to do:

### Milestone 2: Construct New Sequences

1. Add a custom test case to `SplicingAndDicing.cpp` to test the `toStrand` function.
2. Implement `toStrand` and test it thoroughly.

Some notes on this problem:

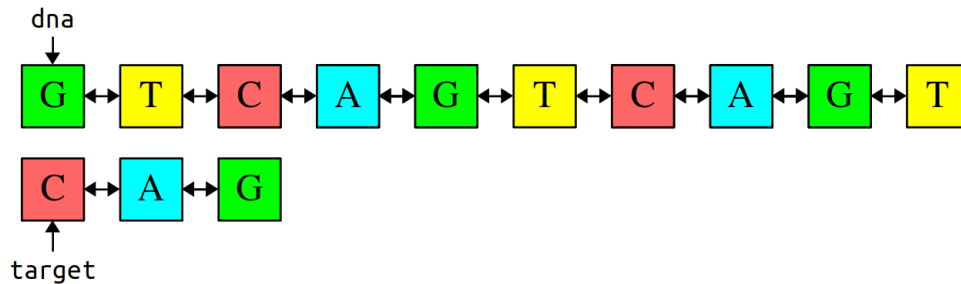
- Remember that the linked list you produce should be a doubly-linked list. This will require you to do some extra wiring in your `toStrand` function.
- Don't be afraid to set breakpoints in test cases and pull up the debugger if you need to figure out where a crash comes from or why your code isn't working. After working through the labyrinth exercises, you should have all the tools you need to reconstruct the state of memory on a sheet of paper. More generally, we recommend that you *never* run your program using the regular "run" button and *always* run with the debugger turned on so that if anything bad happens, you can poke around and see where things went wrong.
- Your implementation of this function should run in time  $O(n)$ . If you're able to pass the provided stress tests, with each one taking at most a few seconds, you should be in good shape.
- This function must work correctly on large inputs. This likely means that you won't be able to implement it recursively, since doing so would lead to stack overflows on long strands.
- You **must not** use any of the container types (e.g. `Vector`, `HashSet`, etc.) in the course of solving this problem. See if you can do this purely using linked lists.

### Milestone Three: Implement Searching

Your next task is to implement a function

```
Nucleotide* findFirst(Nucleotide* dna, Nucleotide* target);
```

that searches for a copy of the strand given by `target` inside the strand given by `dna`, then returns a pointer to the first cell in the match. For example, given these DNA strands, `findFirst` should return a pointer to the third nucleotide in the `dna` list.



(As before, we aren't drawing the null pointers that appear as the `next` and `prev` pointers of the first and last elements of the DNA strands.)

If the sequence given by `target` doesn't appear in `dna`, this function should return `nullptr` to indicate that the sequence wasn't found.

Here's the requirements for this milestone:

#### Milestone 3: Implement Searching

1. Add at least one custom test case to `SplicingAndDicing.cpp` for `findFirst`.
2. Implement the `findFirst` function and test it thoroughly.

Some notes on this problem:

- The `target` sequence could be empty, in which case this function should report that `target` appears at the start of `dna`. This is similar to what you'd do if you wanted to search for the empty string inside of another string: it always exists, and it's always at the front.
- You can assume the `Nucleotide` objects that make up the `target` sequence are different objects than the `Nucleotide` objects that make up `dna`. That is, the `target` pointer doesn't point into the middle of `dna`. More generally, you can assume the pointers passed into this function always point at the start of the lists in question.
- You should not allocate any memory with `new` in the course of implementing `findFirst`, since you're not actually creating any new nucleotides. Feel free to declare variables of type `Nucleotide*` (remember that creating a pointer is separate from using the `new` keyword), but don't use the `new` operator.
- Your code should be efficient enough to pass the test cases that we've bundled with the starter files, but aside from that we won't set any specific big-O target runtime.
- Your functions should work on input sequences of any length, including very long sequences. This will likely preclude the use of recursion here, since you might run out of stack space on those large sequences.
- You **must not** use any of the container types (e.g. `Vector`, `HashSet`, etc.) in the course of solving this problem. See if you can do this purely using linked lists.

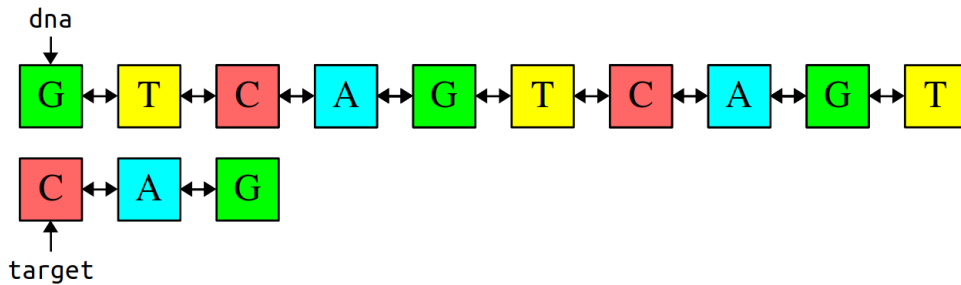
### Milestone Four: Implement Splicing

Your last task is to write a function

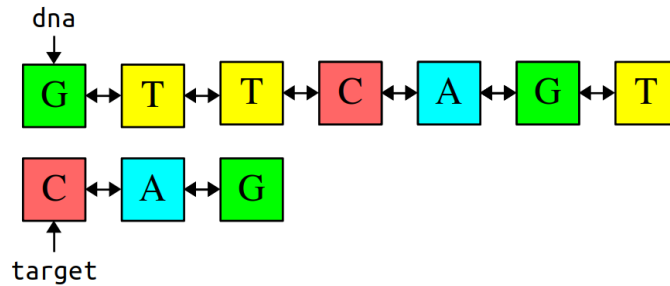
```
bool spliceFirst(Nucleotide*& dna, Nucleotide* target);
```

that takes as input two DNA strands. The first strand, `dna`, is the DNA sequence to search. The second strand, `target`, is a specific sequence to chop out of the DNA strand. Your function should then find the first copy of `target` inside of `dna`, then edit the `dna` strand by removing that sequence in its entirety. If that sequence doesn't exist, this function should return false to indicate that nothing was removed.

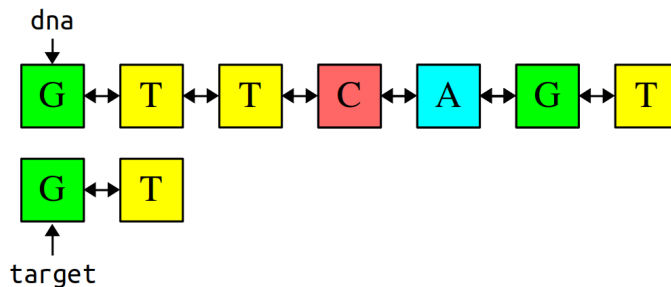
For example, suppose we have these strands:



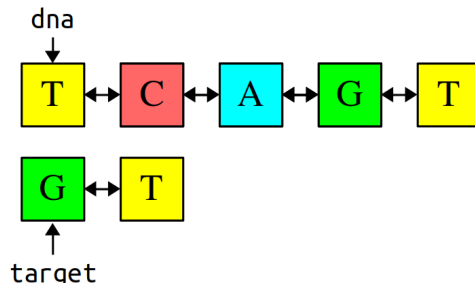
As before, we aren't drawing the null pointers that appear as the next and prev pointers of the first and last elements of the DNA strands. Calling `spliceFirst(dna, target)` would give this result:



The first copy of "CAG" was deleted from `dna`, though the second copy of "CAG" still exists; `spliceFirst` only removes the first copy of `target`. On the other hand, suppose we have these sequences:



Calling `spliceFirst(dna, target)` would result in the following:



Notice that `dna` has changed to point later in the sequence, since we deleted the beginning of the strand.

Given this, here's your next milestone:

#### ***Milestone 4: Implement Splicing***

1. Add at least one custom test for the `spliceFirst` function.
2. Implement the `spliceFirst` function and test it thoroughly.

Some notes on this problem:

- Your function should leave the original strand unchanged except for the removed section and possibly the `Nucleotides` that appear just before and just after that section. In other words, you should only make local modifications to the strand rather than, say, allocating a new strand or changing which characters are stored in which `Nucleotide` objects.
- You can assume that `Nucleotide` objects that make up the `target` sequence are different objects than the `Nucleotide` objects that make up `dna`. That is, the `target` pointer doesn't point into the middle of `dna`.
- Your implementation of `spliceFirst` should not leak any memory. In particular, if you remove any nucleotides from the DNA strand, you should be sure to `delete` them.
- You may have noticed that the `dna` parameter is passed by reference (i.e. `Nucleotide*&` rather than `Nucleotide*`). This is because you may need to change where the `dna` pointer points; specifically, if you remove the first nucleotide from the strand, you will need to reassign `dna` to point after the removed sequence. Be careful not to change where `dna` is pointing unless you're removing something from the front of the sequence.
- The target sequence could be empty, in which case this function should simulate removing nothing from the DNA strand. Specifically, your function should leave the DNA strand unmodified and return `true` to indicate that, indeed, zero nucleotides were removed from it.
- You should not allocate any memory using `new` in the course of implementing `spliceFirst`, since you're not actually creating any new nucleotides. Feel free to declare variables of type `Nucleotide*` (remember that creating a pointer is separate from allocating memory using `new`), but don't use the `new` operator.
- As before, you should not implement this function recursively because we might be running huge DNA sequences through it and you won't have the stack space to pull this off.
- If, in the course of coding this one up, you start seeing crashes or bugs in `fromDNA`, `deleteNucleotides`, or `findFirst`, it could mean either that there's a bug in your `spliceFirst` function that caused the list to be wired improperly or that there was a lurking issue in one of those earlier functions that accidentally sneaked past the tests from the earlier milestones. In other words, don't immediately assume that one of the earlier functions is the culprit; investigate `spliceFirst` as well to make sure that it didn't leave the wiring between the nucleotides in a bad state.
- ***The debugger is your friend!*** Don't hesitate to set breakpoints in test cases or step through your code if you find any issues with your program; this is a *great* way to see what your code is doing. You learned how to sketch out how linked structures look in memory when working through the labyrinth escape, and those same skills will be useful to you here.
- Your code should be efficient enough to pass the test cases that we've bundled with the starter files, but aside from that we won't set any specific big-O target runtime.
- You ***must not*** use any of the container types (e.g. `Vector`, `HashSet`, etc.) in the course of solving this problem. See if you can do this purely using linked lists.

## (Optional) Problem Three: Extensions

This assignment is all about linked structures, and there's plenty of room for you to do Fun and Exciting Things with the topics we've covered here. Here's some thoughts to help get you started, but the sky's the limit here!

- **The Labyrinth!:** Our provided code generates random mazes using combinations of several famous algorithms and data structures. (The normal maze is generated using *Kruskal's algorithm* and a *disjoint-set forest*, the twisted maze is generated using an *Erdős-Rényi random graph* with connectivity guaranteed via *breadth-first search*, and the starting locations are chosen by a procedure that uses the *Floyd-Warshall algorithm* as substep.) There are lots of fairly accessible articles online about how to generate random mazes in other ways. For example, you can use a *randomized depth-first search* to build mazes with lots of long, twisted hallways, or *randomized Prim's algorithm* to build mazes that branch out from a central location. *Wilson's algorithm* produces mazes that are sampled uniformly at random from the space of all possible mazes. Play around with these and see what you find!

Other things you could consider: could you build a visualizer that draws the maze given a pointer to your starting location? Or could you write a program that automatically finds the shortest paths out of a maze?

- **Splicing and Dicing:** DNA often comes in the form of *plasmids*, in which the DNA links in a ring rather than having a definitive beginning and end. Adapt the functions you wrote earlier to work in the case where the input strands are plasmids in addition to regular DNA strands.

There are a number of algorithms you can use to implement `findFirst` in time  $O(m + n)$ , where  $m$  is the length of the DNA strand / plasmid to process and  $n$  is the length of the target sequence. (This is as fast as you can make this algorithm – anything shorter than this means that you can't even read the whole DNA sequence and target, something you'd need to do in the worst case). The *Knuth-Morris-Pratt (KMP)* algorithm guarantees this worst-case performance. The *Rabin-Karp* algorithm uses hash functions in a really clever way that gives an average-case performance of  $O(m + n)$ , though with a worst-case performance of  $O(mn)$ . Explore these algorithms and see what you find!

## Submission Instructions

Once you've autoindented your code so that it looks beautiful and worked through the Assignment Submission Checklist, submit the following files on Paperless, plus any other files you modified when writing up extensions:

- `Labyrinth.cpp`.
- `LabyrinthEscape.cpp`.
- `SplicingAndDicing.cpp`.

And that's it! You're done! You've gotten comfortable working with linked structures and are now much more comfortable working with the debugger. Nicely done!

*Good luck, and have fun!*